Periodicity in the BrO/SO$_2$ molar ratios in the volcanic gas plume of Cotopaxi and its correlation with the Earth tides during the eruption in 2015

Florian Dinger$^{1,2}$, Nicole Bobrowski$^{1,2}$, Simon Warnach$^{1,2}$, Stefan Bredemeyer$^3$, Silvana Hidalgo$^4$, Santiago Arellano$^5$, Bo Galle$^5$, Ulrich Platt$^{1,2}$, and Thomas Wagner$^1$

$^1$Max-Planck Institut for Chemistry, Mainz, Germany
$^2$Institute for Environmental Physics, University of Heidelberg, Germany
$^3$GEOMAR, Kiel, Germany
$^4$Instituto Geofísico, Escuela Politécnica Nacional, Quito, Ecuador
$^5$Department of Earth and Space Sciences, Chalmers University of Technology, Gothenburg, Sweden

Correspondence to: Florian Dinger (florian.dinger@mpic.de)

Abstract. We evaluated NOVAC (Network for Observation of Volcanic and Atmospheric Change) gas emission data from the 2015 eruption of Cotopaxi volcano (Ecuador) for BrO/SO$_2$ molar ratios. Statistical analysis of the data revealed a conspicuous periodic pattern with a periodicity of about two weeks in a three month time series. While the time series is too short to rule out a chance recurrence of transient geological or meteorological events as a possible origin for the periodic signal, we nevertheless took this observation as a motivation to examine the influence of natural forcings with periodicities of around two weeks on volcanic gas emissions. One strong aspirant with such a periodicity are the Earth tides, which are thus central in this study. We present the BrO/SO$_2$ data, analyse the reliability of the periodic signal, discuss a possible meteorological or eruption-induced origin of this signal, and compare the signal with the theoretical ground surface displacement pattern caused by the Earth tides. Central result is the observation of a significant correlation between the BrO/SO$_2$ molar ratios with the North-South and vertical components of the calculated tide-induced surface displacement with correlation coefficients of 47% and 36%, respectively. From all other investigated parameters, only the correlation between the BrO/SO$_2$ molar ratios and the relative humidity in the local atmosphere resulted in a comparable correlation coefficient of about 33%.

1 Introduction

Magmatic melts are a reservoir of dissolved volatile species. Typically, the dominant part of those volatiles is water vapour followed by carbon dioxide and sulphur compounds but also a large number of trace gases like halogen compounds. The solubility of volatiles in magmatic melts is primarily pressure dependent with secondary dependencies on temperature, melt composition, and volatile speciation (Gonnermann and Manga, 2013). Monitoring the magnitude and composition of volcanic gas emissions has the potential to give insight in those geological processes which vary the solubility regime within a volcanic system. Because the pressure-dependency of the volatile solubility is different for each particular volatile species, among others, halogen to sulphur molar ratios in volcanic gas plumes are discussed as accessible and suitable proxies for the magma...
pressure or the degassing depth, e.g. Edmonds et al. (2001) for chlorine to sulphur ratio, Bobrowski and Giuffrida (2012) for bromine to sulphur ratio.

While in-situ gas measurements allow for a composition analysis of volcanic gas emissions for a broad spectrum of elements and compounds, such measurements are usually not suited to estimate by themselves the magnitude of volcanic emissions and an automatic daily sampling is only possible for few species and requires high and often cost intensive maintenance efforts.

The development of remote sensing techniques such as passive Correlation Spectroscopy (COSPEC, M. M. Millan (1970)) and Differential Optical Absorption Spectroscopy (DOAS, Platt et al. (1980), Platt and Stutz (2008)) allow for recording semi-continuous (only during daytime) time series of the magnitudes of volcanic gas emissions as well as analyses of the shape and transport of volcanic gas plumes. However, also monitoring by remote sensing was initially performed only manually, thus rarely done and the time series were often limited to several weeks (with few exceptions e.g. Caltabiano et al. (1994)). This changed with the installation of an automatic measurement network at Soufriere Hills volcano at Montserrat in 2002 which produced semi-continuous time series with a time resolution of about 6 minutes by scanning in 4.5° steps with a small field of view telescope from horizon to horizon (Edmonds et al., 2003). In 2005, this network design was extended to a larger scale by the Network for Observation of Volcanic and Atmospheric Change (NOVAC, Galle et al. (2010)) for automatic monitoring of volcanic SO\textsubscript{2} emissions, which was funded by the European Union and whose stations are predominately installed in South and Central America. Similar networks are installed at individual volcanoes, e.g. Strombolli and Mt. Etna (FLAME network, Burton et al. (2009), Salerno et al. (2009)), Kilauea (FLYSPEC, Businger et al. (2015)), and White Island (Miller et al., 2006).

As a drawback, usually remote sensing techniques are only sensitive for those trace gas species which are characterized by differential absorption structures and which are sufficiently abundant in the volcanic gas plume (i.e. whose structured absorption in the UV/visible spectral range exhibits an optical density of at least \(10^{-3}\)). Furthermore, the measurements sometimes might be influenced by variations in the meteorological conditions, especially the atmospheric visibility. Further, it is challenging to observe the emission of the two major volcanic gas compounds, water vapour and carbon dioxide, because for these gases the additional volcanic contribution to the absorption signal is typically tiny compared to their atmospheric background level. The set of retrievable trace gases is limited to the wavelength range of the particular spectrometer. The NOVAC data are recorded by UV-spectrometers with a usable wavelength range from 280 nm to 360 nm, which allows - in its current state - for an automated retrieval of the volcanic trace gas concentrations of SO\textsubscript{2} and BrO in the volcanic gas plumes.

While SO\textsubscript{2} is directly emitted from the volcano and is assumed to have a lifetime of hours to days (e.g. Beirle et al. (2014), Fioletov et al. (2015)), volcanic bromine is considered to be predominately emitted as hydrogen bromine (HBr) and gets only partially converted by photochemistry to BrO by the so-called bromine explosion process (e.g. Platt and Lehrer (1997), Wennberg (1999), von Glasow (2010)). The equilibrium of the conversion \(\text{HBr} \rightleftharpoons \text{BrO}\) is typically reached already within the first minutes after the release of HBr to the atmosphere (Platt and Bobrowski (2015), Gliß et al. (2015)). The NOVAC-instruments (typically installed 5 – 10 km downwind of the crater and thus observing plumes with an age of about 10 – 30 min) scan through volcanic gas plumes which are expected to have already reached the BrO equilibrium. The conversion rate or even the stationary state ratio between HBr and BrO may depend on the plume composition and the atmospheric conditions (meteorology) (Roberts et al., 2014) and thus on parameters like solar irradiance, air temperature, air pressure, or relative hu-
midity. However, Bobrowski and Giuffrida (2012) have not found a correlation between BrO and the relative humidity or the wind speed, which poses the question if the bromine explosion in volcanic gas plumes is indeed significantly depending on the meteorological conditions or not.

To summarise, NOVAC data is used to retrieve volcanic SO$_2$ emission fluxes and BrO/SO$_2$ molar ratios (Lübcke et al., 2014) in volcanic plumes. Because BrO is about four orders of magnitude less abundant in the volcanic plume than SO$_2$, the retrieved BrO data is often close to the detection limit and thus the BrO/SO$_2$ time series are less continuous than the SO$_2$ emission flux estimates. On the other hand, the accuracy of SO$_2$ emission flux estimates may experience high uncertainties due to the atmospheric radiative transport (e.g. Mori et al. (2006), Kern (2009)) while these effects approximately cancel when calculating the BrO/SO$_2$ molar ratio (Lübcke et al., 2014). Finally, for an accurate volcanological interpretation of the NOVAC data, information on the meteorological conditions have to be included in both analyses as the calculation of SO$_2$ emission fluxes requires wind information and the steady state HBr $\rightleftharpoons$ BrO may depend on the atmospheric conditions.

Today, NOVAC encompasses about 100 automatically measuring optical UV-spectrometers at 41 volcanoes and with a mean temporal resolution of one horizon to horizon scan about every 10 min. The large data set of more than 10 years of semi-continuous time series of volcanic SO$_2$ emission fluxes as well as time series of the BrO/SO$_2$ molar ratios allow for a statistical investigation of long-term signals in the volcanic degassing and a comparison with other long-term signals as well as a comparison between different volcanoes. Conde et al. (2014) observed a periodic pattern of roughly 13 days in the NOVAC SO$_2$ emission fluxes from Turrialba (Costa Rica) which was suggested by the authors to be caused by a pressure change due to the Earth tidal forcing. Bredemeyer and Hansteen (2014) used NOVAC data from Villarrica and Llaima (both southern Chile) to investigate a possible correlation between their SO$_2$ emission fluxes and the surface displacement due to the Earth tides and report correlation coefficients of up to 20 % and 30 %, respectively. In this manuscript we retrieve the variation of the BrO/SO$_2$ molar ratios recorded by NOVAC during the 2015 period of unrest at Cotopaxi volcano (e.g. Bernard et al. (2016), Gaunt et al. (2016), Morales Rivera et al. (2017)) and examine a correlation between its variation and variations in the meteorological and geological conditions, including the calculated variations of the Earth tide-induced ground surface displacements.

2 Cotopaxi

2.1 Geology and volcanism at Cotopaxi

Cotopaxi (-0.7°S, 78.4°W, 5897 m a.s.l.) is a glacier-capped stratovolcano located in the Ecuadorian inter-Andean valley, a N-S to NNE-SSW trending topographical depression. Volcanism in this area is caused by the oblique subduction of the Nazca plate beneath the South American plate, which experiences intense large-scale deformation leading to shortening of the lithosphere along the Andean orogeny (e.g. Trenkamp et al. (2002), Alvarado et al. (2016)). The volcano lies on a fault transfer zone (e.g. Gibbs (1990)) in which E-W striking normal faults and NNE-SSW-striking vertical, right-lateral oblique strike-slip faults accommodate the differential crustal shortening rates encountered North and South of Cotopaxi (Fiorini and Tibaldi, 2012). Fiorini and Tibaldi (2012) thus proposed that the fault planes and restraining bends of this transfer zone act as the main magma pathways feeding the volcano. Within the last 0.5 Ma, a rhyolitic and andesitic bimodal magmatism has occurred at Cotopaxi
The Smithonian Institution (http://volcano.si.edu/) lists 55 eruptions at Cotopaxi within the last 300 years, with the last confirmed eruption in 1940 (VEI 2) or, an unconfirmed eruption in 1942 (VEI 3), and the last major (VEI 4) eruption in 1877. The major hazard of an eruption from Cotopaxi consists in the generation of lahars as a consequence of melting the snow and ice of the summit glacier (Barberi et al., 1995). During the 1877 eruption the glacier of Cotopaxi has completely been molten by the expelled pyroclastic flows, producing devastating lahars which traveled down the flanks of the volcano and destroyed e.g. the town of Latacunga located about 30 km South of the volcano (Aguilera et al., 2004). Later activity of Cotopaxi did not involve melting of the glacier, which thus recovered since then.

2.2 Predicted Earth tidal surface displacement at Cotopaxi location

The tidal forces periodically displace the Earth’s surface and interior, a summary of the theory of the Earth tides can be found in Appendix A. The periodicities and magnitudes of the tide-induced surface displacement patterns at Cotopaxi are plotted in Figure 1 (predicted with the GNU R software using the package from Gama and Milbert (2015)). The vertical surface displacements vary by up to $\pm 0.3$ m within a day and follow a semi-diurnal periodicity (Figure 1, hourly-resolved data in the upper panel). The semi-diurnal peak-to-peak variation (calculated as the maximum difference within a sliding window of 13 h) of the vertical surface displacements varies between $0.15 - 0.55$ m with a maximum every 14.75 days (Figure 1, red line in upper panel). For ocean tides, this long-term periodicity is called spring-neap tidal cycle, a labelling which we adopt in this paper also for the Earth tides, i.e. maximum daily variations during a spring tide and minimum daily variations during a neap tide. Notably, each second spring tidal maximum is relatively small because the tidal forcing is slightly stronger during new moon compared with full moon. The Earth tides also result in horizontal displacements (see Figure 1 lower panel). Near the equator, where Cotopaxi is located, the East-West displacement is a factor of 5 and the North-South displacement is a factor of 10 smaller than the vertical displacement but for higher latitudes these ratios differ. The East-West component of the tide is in phase with the vertical component (see also Figure 5) but the North-South component has a smaller and less regular periodicity of about 13-14 days. Furthermore, all tidal components have an annual modulation in the mean displacement with a maximum (for the vertical component) or minimum (for the North-South component) variation in late September 2015.

2.3 Cotopaxi’s recent unrest and eruption

Around early April 2015 the seismic event rate started to increase which signalised a new period of unrest. From mid May 2015 on, also the observed volcanic degassing of SO$_2$ and BrO increased to significant levels above the detection limit (Figure 3). On August 14 2015 several phreatomagmatic explosions opened the conduit resulting in continuous ash emissions and large gas emissions. The period of unrest and eruptions was monitored by the broad network of different sensors maintained by the local observatory IGEPN in Quito which published the accumulated data as well as interpretations already in scientific papers. Those based on a comparison of the temporal variations of magnitude (Bernard et al., 2016) and composition (Gaunt et al., 2016) of ash emissions as well as ground deformation (Morales Rivera et al., 2017) with seismic signals, SO$_2$ emission fluxes, and general visual observations. Morales Rivera et al. (2017) report a maximum uplift of 3.4 cm at the western flank of Cotopaxi from April to August 2015 while they observed no further significant deformation after the eruption in August.
Figure 1. Time series of the vertical (top panel and red line in bottom panel) and horizontal (blue and green lines of the lower panel) components of the ground surface displacement at Cotopaxi due to the Earth tides. Upper panel: Hourly resolved vertical surface displacements (black, left ordinate axis) and its daily peak-to-peak variation (red, right ordinate axis). Lower panel: Time series of the daily peak-to-peak variation for all three spatial directions. Vertical and East-West components of the tide are in phase and have a periodicity of 14.75 days. The North-South component of the tide has no unique periodicity but a mean periodicity of 13-14 days and is increasing from September to December 2015.

The authors explain the deformation by an inclined sheet intrusion located a few km southwest of the summit. Bernard et al. (2016) and Gaunt et al. (2016) agree in the division of the post-explosion dynamics in four phases: August 14-15 (phase 1), August 15 to October 2 (phase 2), October 2 to November 4 (phase 3), and November 4-11 (phase 4). In phase 1, several phreatomagmatic explosions occurred followed by ash clouds reaching altitudes of 9.3 km above the crater and strong gas emissions. During phase 2, continuous but decreasing ash emissions were observed. In the first half of phase 2, the number of seismic long-period events as well as the amplitude of tremor was the highest of the overall period of unrest. In Phase 3, tremor and magnitude of ash emissions increased again and peaked in mid of October. In phase 4, only little ash was emitted and the ash plumes did not exceed 2.5 km above the crater.

Gaunt et al. (2016) suggest an intrusion of juvenile magma in a shallow reservoir (less then 3 km depth) since April 2015 as
the reason for the reawakening of Cotopaxi, a suggestion backed by the findings of Morales Rivera et al. (2017). The juvenile magma may have started to heat an overlying hydrothermal system which may ultimately resulted in dry degassing pathways, an interpretation which fits to the observation of shallow SO$_2$ degassing from May 2015 on. The phreatomagmatic explosions removed the plug which consisted of old, altered material. After the explosions, the magma ascent slowed down and/or the residence times at shallow levels increased. As the crystallinity increased, the magma stiffened and a new shallow plug was formed. The authors further highlighted that the fragmentation mechanisms during phase 2 to 4 are not fully understood. Especially the continuous fine ash grain size distribution throughout all phases suggest that several fragmentations took place. As possible interpretation, the authors suggest a repetitive formation and destruction of shallow plugs.

3 DOAS measurements of SO$_2$ and BrO

3.1 NOVAC stations at Cotopaxi

Today four NOVAC stations are installed around Cotopaxi at distances of 2 to 15 km, predominately downwind (Figure 2). The stations Refugio (instrument no.: D2J2160) and NASA (I2J4969) have operated since 2008. In August 2015, the instrument I2J4969 was relocated from NASA station to the more distantly located new San Joaquin station because the former became unsuitable due to increased ash precipitation. In October 2015, the stations Refugio Sur (D2J2815) and Cami (D2J2835) were additionally installed.

3.2 SO$_2$ and BrO time series during the Cotopaxi 2015 period of unrest

We used Differential Optical Absorption Spectroscopy (DOAS) in order to retrieve SO$_2$ and BrO gas emissions from NOVAC data taken during the Cotopaxi period of unrest and eruption (May 2015 - April 2016). Our evaluation is based on Lübcke et al. (2014) but with a modified plume detection algorithm and the option to switch the SO$_2$ fit range when extreme SO$_2$ emissions are observed (see for both issues Appendix B). The output of the evaluation are time series of the slant column densities (SCD) of SO$_2$ and BrO as well as time series of the daily averages of the BrO/SO$_2$ molar ratio in the centre of the volcanic gas plume. SO$_2$-SCDs are the raw data which pose, combined with information of the plume expansion and the wind conditions, the data base for SO$_2$ emission flux estimations. Accordingly, under stable meteorological condition (similar plume extension and wind speed) SO$_2$-SCDs and SO$_2$ fluxes are highly correlated and share similar long-term behaviour.

Prior to May 2015, Cotopaxi was limited to fumarolic degassing and no significant gas plume was detected since the installation of the NOVAC instruments in 2008 (SO$_2$-SCDs $\leq 2 \cdot 10^{17}$ molec cm$^{-2}$ and BrO-SCDs were below the detection limit of $3 \cdot 10^{13}$ molec cm$^{-2}$, i.e. twice the standard deviation, first and second panel in Figure 3). Between mid May 2015 and the phreatomagmatic explosions on August 14 2015 the SO$_2$-SCDs increased up to $2 \cdot 10^{18}$ molec cm$^{-2}$ and the BrO-SCDs increased up to $7 \cdot 10^{13}$ molec cm$^{-2}$. Within this period, the calculated BrO/SO$_2$ molar ratios were extremely low with an average of $0.16 \pm 0.13 \cdot 10^{-5}$ (third panel in Figure 3). No variations can be resolved because the values are close to the BrO detection limit. Within the week directly after the phreatomagmatic explosions on August 14 2015, mean SO$_2$-SCDs of $2 \cdot 10^{18}$ molec cm$^{-2}$ were
Figure 2. Location and scan geometries (see details in Galle et al. (2010)) of the four NOVAC stations at Cotopaxi volcano, the colours match to the time series in Figure 3. After the phreatomagmatic explosions on August 14 2015 the instrument I2J4969 was relocated from NASA station to San Joaquin station. The wind rose in the right bottom corner illustrates the typical wind conditions in an altitude of 100 m above the crater, i.e. 6000 m a.s.l. (Map was created with graphical material from Google Earth and wikipedia.com. Wind data were taken from a ECMWF model, see section 4.)

Table 1. Typical SO$_2$-SCDs and BrO-SCDs in the gas plume of Cotopaxi in the year 2015. Except for the first time period, the mean values refer to the data which are filter for the strong plume threshold SO$_2$-SCD $> 7 \cdot 10^{17}$ molec cm$^{-2}$.

<table>
<thead>
<tr>
<th>Time period (in year 2015)</th>
<th>mean SO$_2$-SCD</th>
<th>max SO$_2$-SCD</th>
<th>mean BrO-SCD</th>
<th>max BrO-SCD</th>
<th>mean BrO/SO$_2$</th>
</tr>
</thead>
<tbody>
<tr>
<td>May 1 - May 22</td>
<td>$1 \cdot 10^{17}$ molec cm$^{-2}$</td>
<td>$2 \cdot 10^{17}$ molec cm$^{-2}$</td>
<td>$\approx 0$</td>
<td>$4 \cdot 10^{13}$ molec cm$^{-2}$</td>
<td></td>
</tr>
<tr>
<td>May 22 - August 14</td>
<td>$1 \cdot 10^{18}$ molec cm$^{-2}$</td>
<td>$2 \cdot 10^{18}$ molec cm$^{-2}$</td>
<td>$2 \cdot 10^{12}$ molec cm$^{-2}$</td>
<td>$7 \cdot 10^{13}$ molec cm$^{-2}$</td>
<td>$0.2 \pm 0.1 \cdot 10^{-5}$</td>
</tr>
<tr>
<td>August 14 - August 22</td>
<td>$2 \cdot 10^{18}$ molec cm$^{-2}$</td>
<td>$3 \cdot 10^{18}$ molec cm$^{-2}$</td>
<td>$2 \cdot 10^{13}$ molec cm$^{-2}$</td>
<td>$8 \cdot 10^{13}$ molec cm$^{-2}$</td>
<td>$1.1 \pm 0.2 \cdot 10^{-5}$</td>
</tr>
<tr>
<td>August 22 - September 8</td>
<td>(data gap)</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>September 8 - December 5</td>
<td>$1 \cdot 10^{18}$ molec cm$^{-2}$</td>
<td>$1 \cdot 10^{19}$ molec cm$^{-2}$</td>
<td>$2 \cdot 10^{14}$ molec cm$^{-2}$</td>
<td>$4 \cdot 10^{14}$ molec cm$^{-2}$</td>
<td>$4.8 \pm 1.8 \cdot 10^{-5}$</td>
</tr>
<tr>
<td>December 5 - May 1 2016</td>
<td>$1 \cdot 10^{18}$ molec cm$^{-2}$</td>
<td>$2 \cdot 10^{18}$ molec cm$^{-2}$</td>
<td>$4 \cdot 10^{13}$ molec cm$^{-2}$</td>
<td>$1 \cdot 10^{14}$ molec cm$^{-2}$</td>
<td>$4.4 \pm 1.6 \cdot 10^{-5}$</td>
</tr>
</tbody>
</table>
Figure 3. Three upper panels: Time series of the slant column densities of SO₂ and BrO and calculated BrO/SO₂ molar ratios in the gas plume emitted from Cotopaxi (tick marks indicate first day of the particular month). The NOVAC stations are indicated by the different colours. Lowest panels: Lomb-Scargle frequency component analysis and time-lag auto-correlation coefficients of the BrO/SO₂ molar ratio variations. Both analyses are based on the (not trend-corrected, i.e. “as shown”) data acquired during the time interval indicated by the running mean line in the BrO/SO₂ molar ratio plot. The dashed lines give the 1% significance level and the 90% confidence level, respectively. All minor peaks in the Lomb-Scargle periodigram are most probable just artefacts due to a spectral leakage from the peak at 13.7 days.
observed with a maximum value of \(3 \cdot 10^{18} \text{ molec cm}^{-2}\), the mean BrO-SCDs increased from approximately 0 to \(2 \cdot 10^{13} \text{ molec cm}^{-2}\), to a maximum of \(8 \cdot 10^{13} \text{ molec cm}^{-2}\), and a mean BrO/\text{SO}_2 molar ratio of \(1.1 \pm 0.2 \cdot 10^{-5}\) was derived. From August 22 to September 8 2015, there are only sparse plume data recorded because the solar panel at NASA station was temporarily covered by ash and the gas plume was apparently not transported through the field of view of the Refugio station during this period. After September 8 2015, a drop in the \text{SO}_2-SCDs derived from the data measured at the NASA and San Joaquin stations (green dots in Figure 6) is expected independently from a possible variation of the volcanic degassing behaviour. The reason is the relocation of the instrument to a larger distance to the emission source and therefore observing more diluted volcanic gas plumes.

From early September 2015 to mid of December 2015, the mean \text{SO}_2-SCDs remained approximately on the same level as directly after the explosions (significant amount of data above \(1 \cdot 10^{18} \text{ molec cm}^{-2}\) but typically below \(3 \cdot 10^{18} \text{ molec cm}^{-2}\), however with strong temporal variability (compared to the emission before September 2015) with a maximum of \(13 \cdot 10^{18} \text{ molec cm}^{-2}\). In contrast, much higher BrO-SCDs were observed in this period with daily maxima typically varying between \(1 - 2 \cdot 10^{14} \text{ molec cm}^{-2}\) but up to \(4 \cdot 10^{14} \text{ molec cm}^{-2}\). As expected with respect to the gas plume dilution, an intercomparison of the data obtained from the different stations reveals that the observed SCDs in both \text{SO}_2 and BrO are larger the closer the station is to the edifice of Cotopaxi, however, all stations observed similar BrO/\text{SO}_2 molar ratios. Further, Refugio station which is installed just 2 km North of Cotopaxi observed some extreme SCD-values (simultaneously for \text{SO}_2 and BrO) which are not at all observed by the other stations. A comparison with the wind profile (see also Figure 4) revealed that at least three (on September 29, October 9, October 20) of those seven \text{SO}_2-peaks (with \text{SO}_2-SCDs > \(7 \cdot 10^{18} \text{ molec cm}^{-2}\)) coincide with extreme low wind speeds (< 2 m s\(^{-1}\)), thus at those days the elevated SCDs may be caused by an accumulation of the volcanic gas emissions in proximity to the crater. Accumulated gas plumes are expected to have a reduced BrO/\text{SO}_2 molar ratio due to the limited lifetime of BrO. For the three mentioned days, the mean BrO/\text{SO}_2 molar ratios indeed dropped to \(2 \cdot 10^{-5}\), thus despite the observed large BrO-SCDs, we have to be cautious when interpreting the BrO/\text{SO}_2 molar ratios of those days. Within the period from early September 2015 to early December 2015 a mean BrO/\text{SO}_2 molar ratio of \(4.8 \cdot 10^{-5}\) but with variations from \(1 - 12 \cdot 10^{-5}\) was observed. Further, the BrO/\text{SO}_2 molar ratios increased from early September 2015 on with a trend of about \(0.3 \cdot 10^{-5}\) per month. Since early December 2015 the mean \text{SO}_2-SCDs dropped to levels comparable to those prior to the explosions, however, with some minor \text{SO}_2 degassing events which were detected exclusively by the Refugio station. Also the mean BrO-SCDs dropped to \(1 \cdot 10^{13} \text{ molec cm}^{-2}\), i.e. below the detection limit, however, in contrast to the situation prior to the explosions for most days daily maxima above the detection limit were observed with values of even up to \(1 \cdot 10^{14} \text{ molec cm}^{-2}\) on few days.

### 3.3 Periodic pattern in the BrO/\text{SO}_2 molar ratios after the explosions

Within the time interval from early September 2015 to early December 2015, the highly significant BrO absorptions and the up to four simultaneously monitoring NOVAC stations yield an extraordinarily good temporal resolution of the BrO/\text{SO}_2 time series of almost daily resolution. Therefore besides the monotonous long-term trend also "high-frequent" (with periods of weeks or months) variations can be resolved in the BrO/\text{SO}_2 data. And indeed, the maxima and minima of the BrO/\text{SO}_2 molar ratios apparently follow a periodic pattern with a period of about two weeks and an amplitude (of the smoothed data) of about \(1 \cdot 10^{-5}\), i.e. a relative variation of about 20%, as illustrated by the running mean over 7 days (third panel in Figure 3).
In order to examine a quantitative estimation for the reliability of this signal we tested two statistical methods, a Lomb-Scargle frequency component analysis (Lomb (1976), Scargle (1982), Press et al. (1992), in the following just called Lomb-Scargle analysis) as well as an (time-lag) auto-correlation analysis. Compared with a common Fourier transform analysis those two methods can more appropriately handle time series with irregular sampling intervals, a problem we are facing as long as we are not interpolating the BrO/SO$_2$ molar ratio time series at the missing days. Namely, the Lomb-Scargle analysis is similar to a Fourier transform analysis but explicitly designed for the examination of irregularly spaced time series and while the auto-correlation analysis still requires a linear interpolation of the BrO/SO$_2$ time series the distortion on the correlation coefficients is much weaker than for a Fourier transform analysis based on sinusoidal signals. Both methods were applied to the daily data (arithmetically averaged over all instruments when daily means were available for several instruments) for the time interval from September 8 2015 to December 15 2015 (as illustrated by the black line of the running mean in the third panel of Figure 5). The first week of September 2015 and the first week of December 2015 were excluded from both analyses as the temporal resolution is much worse at those times. Also the trend was removed by subtracting a polynomial fit to the fifth order from the BrO/SO$_2$ time series. The Lomb-Scargle analysis proposes a periodicity of 13.7 days and the auto-correlation analysis confirms the existence of a periodicity of 13-14 days (lowest panels in Figure 3). For both methods, the results are highly significant (Lomb-Scargle false alarm probability of 0.9 % and an auto-correlation detection confidence of about 90 %, respectively) and thus the periodic signal is with high probability an observation of a natural process (or a series of those) rather than statistical noise.

4 Meteorological conditions during the Cotopaxi eruption

The atmospheric chemistry and meteorological conditions may have an impact on the BrO/SO$_2$ molar ratios observed in volcanic gas plumes (see introduction). Unfortunately, direct measurements of the meteorological conditions at volcanoes, and in particular at the altitudes of volcanic plumes, are scarcely or not at all available. A quantification of the sky cloudiness or the aerosol load in a volcanic plume may be retrieved directly from the spectroscopic data by well-established methods such as an analysis of variations in the oxygen dimer O$_4$ absorption or an analysis of the so-called colour index (Wagner et al., 2014). However, the spectra recorded by NOVAC do not allow for an application of the the validated versions of those methods because the spectral properties are optimised for a retrieval of SO$_2$ and BrO, thus for a wavelength range below 360 nm. In contrast, the O$_4$ analysis requires spectra of good quality also at longer wavelengths. Analyses with modified versions of those methods (see Appendix B4) did not found any reliable pattern in the time series of the sky cloudiness. Weather forecast models pose the best available proxy for the meteorological conditions around the volcanic gas plume. We use operational analysis data from ECMWF (on a Gaussian Grid N640 and with a T1279 truncation) with a spatial resolution of 0.14° x 0.14° and a temporal resolution of 6 h (0:00, 6:00, 12:00, and 18:00 UTC) and picked the model altitude around 6000 m a.s.l. (100 m above the crater, where we roughly expect the volcanic gas plume) in order to get a rough idea of the meteorological variation at Cotopaxi volcano. From the list of available model parameters, we selected 1) the air temperature, the air pressure, and the relative humidity in order to investigate their possible influence on plume chemistry, 2) the wind speed...
and wind direction in order to reconstruct the plume transport (and therefore plume age), and 3) the total cloud cover as a poor but still most suited proxy for the radiative conditions. The total cloud cover gives a relative value (from 0 to 1) for the cloud thickness above a pixel integrated from ground up to an altitude of 60 km. However, a total cloud cover of 1 does not necessarily indicate the presence of an optical dense cloud cover close to the ground, but rather indicates whether significant light scattering within clouds has occurred somewhere above the ground pixel. At the equator, where Cotopaxi is located, the total cloud cover is typically close to 1. For our comparison of gas and meteorological data we chose to focus on the data obtained at 18:00 UTC, i.e. 13:00 local time, which match the observation time of the DOAS measurement the best, especially when we compare with the daily averages of the BrO/SO$_2$ molar ratios which are centred around noon time.

During the period of unrest, some of the meteorological parameters experienced strong but irregular variations (Figure 4). We applied a Lomb-Scargle analysis and an auto-correlation analysis on the de-trended time series (trend removed by subtracting a polynomial fit to the fifth order from the time series). When applied to the total presented meteorological time series (July 1 2015 to January 1 2016), no persistent periodic pattern were detected. When limiting the analysis to the time interval of the investigated BrO/SO$_2$ data (i.e. from September 8 2015 to December 15 2015), both the variations of relative humidity and cloud cover show noticeable periodic patterns. The relative humidity was at its half-year minimum of 10% in mid September 2015 and increased to its half-year maximum of 96% in mid of October 2015/early November 2015. Further, this trend was superimposed by a significant (Lomb-Scargle: false alarm probability of 1.2 %) periodicity of 13.1 days. The total cloud cover was at its half-year minimum of 0.6 in mid September 2015 and increased to its half-year maximum of (persistently) 1.0 early November 2015. Further, for the time interval from September 2015 to December 2015 a periodicity of 11.6 days was proposed (Lomb-Scargle: false alarm probability of 2.2 %). An auto-correlation analysis confirms the existence of the three noted periodicities, all with a confidence of about 90%. For the other parameters no significant periodic pattern were detected.

5 Discussion

A variation of the BrO/SO$_2$ molar ratio in the volcanic gas plume could be caused by effects in two independent domains: either within the magmatic system, i.e. varying magmatic processes could cause a variation in the HBr/SO$_2$ molar ratio within the volcanic gas emissions; or in the atmosphere where the atmospheric conditions may delay or accelerate the conversion from HBr to BrO or even change the chemical steady state ratio between HBr (or other bromine compounds) and BrO.

We observed three significant variations in the BrO/SO$_2$ data: (1) an abrupt increase in the molar ratios within September 2015 (unfortunately the exact behaviour is hidden by the data gap), (2) an increasing trend from September 2015 to December 2015, and (3) the periodic pattern from September 2015 to December 2015. In the following we compare the variations in the volcanological, meteorological, and calculated tidal data with the variations in the BrO/SO$_2$ data. For the time interval from September 8 2015 to December 15 2015, we performed a correlation analysis between the BrO/SO$_2$ data, the meteorological data, and the calculated tidal data. All data sets were left with their longterm trends in order to compare the total variations (see Figure 5). An analogue analysis with trend-corrected data lead to similar results but lower correlation coefficients.
Figure 4. Meteorological conditions at 100 m above the peak of Cotopaxi (6000 m a.s.l.) during the period of unrest. The data are based on operational analysis data from ECMWF with a spatial resolution of 0.14° x 0.14°. The grey lines show the ECMWF data with a temporal resolution of 6 h, given in UTC, the black dots show the data at 18:00 UTC, i.e. 13:00 local "noon" time. Running means of 7 day windows are shown as blue lines for the total data set and as red lines for the noon time data, which mostly fall on top of the blue line. The overall long-term trend is indicated by the polynomial fit of fifth order shown in orange. For the wind direction, only data with an easterly component are shown as this is the predominately wind direction (93 % of data) and as westerly components exclusively coincide with low wind speeds (< 4 m/s).
5.1 Comparison of BrO/SO$_2$ time series with meteorology

When limiting the analysed time interval to early September 2015 to mid December 2015, relative humidity, total cloud cover, air temperature, and wind speed show long-term variations (Figure 4), however, those are superimposed by strong short-term variations. For the relative humidity, a frequency analysis finds a significant high-frequent signal with a 13.1 days periodicity which match relatively well the 13.7 days periodicity of the BrO/SO$_2$ data. A cross-correlation analysis of the limited time interval finds a slightly increased correlation coefficient of 33 %. For air temperature, air pressure, and wind conditions no significant periodicities were found and the periodic pattern in the total cloud cover (period of 11.6) does not match with the BrO/SO$_2$ variations. As conclusion, the BrO/SO$_2$ variations may be partially explained by the variations in the relative humidity. However, on the other hand the correlation between the relative humidity and the BrO/SO$_2$ molar ratios may just be caused by a shared dependency on, e.g., the Earth tidal forcing (see good correlation between relative humidity and tide-induced surface displacement in Figure 5).

5.2 Comparison of BrO/SO$_2$ time series with volcanic activity

5.2.1 BrO/SO$_2$ molar ratios as a poorly constrained proxy for volcanic activity

The volatile solubility in magmatic melt can be modelled with high accuracy for water vapour and carbon dioxide (Gonnermann and Manga (2013), Oppenheimer et al. (2014)) and is also relatively well constrained under diverse and variable conditions...
for sulphur (e.g. Scaillet and Pichavant (2005), Moretti and Ottonello (2005), Lesne et al. (2011), Witham et al. (2012)). In contrast, it is more challenging to constrain the halogen behaviour in the melt-fluid phase because of their low abundance in magmatic melt but also because halogens (except fluorine) strongly prefer to partition in the hydrous fluid phase (Bureau et al., 2000). For water-poor magmas, the knowledge is limited to the qualitative observation that halogens typically reach saturation, if at all, at low pressure (Edmonds et al., 2009). For water-rich magmas, the quantitative pressure-dependency of the chlorine solubility in the melt-fluid phase is relatively well constrained (e.g. Carroll (2005), Balcone-Boissard et al. (2016)) and also some insights in the behaviour of the other halogens have been gathered by the experimental (e.g. Bureau and Métrich (2003), Bureau et al. (2010), Bureau et al. (2016)) or empirical (e.g. Villemant et al. (2005), Kutterolf et al. (2015)) derivation of their melt-fluid partition coefficients.

Sulphur and water vapour, and thus also bromine, are predominately degassing after carbon dioxide. Bromine has a larger partition coefficient than chlorine, thus it is reasonable that bromine degasses prior to chlorine. Sulphur is degassing prior to chlorine (e.g. Aiuppa (2009)), however, it is not yet constrained whether sulphur is predominately degassing prior or after bromine. Accordingly, even under the assumption that the HBr/SO$_2$ degassing ratio is purely pressure-dependent no quantitative deduction of the pressure change could be made based on BrO/SO$_2$ molar ratios. Further, it was even not yet possible to derive the sign of this correlation indirectly by empirical studies of BrO/SO$_2$ molar ratios simultaneously to pressure changes (Bobrowski and Giuffrida (2012), Lübcke et al. (2014)) because of the still limited data sets available. In the absence of an explicit interpretation of the BrO/SO$_2$ molar ratio, at least the reasoning that a change in BrO/SO$_2$ molar ratios is probably caused by a significant change in magmatic conditions appears to be nevertheless a reasonable hypothesis. Several studies on BrO/SO$_2$ molar ratios in volcanic gas plumes observed the same pattern that the ratios are relatively low prior and during an eruption but are higher at the end of the eruption or during quiescent degassing periods, e.g. observed at Mt. Etna (Bobrowski and Giuffrida, 2012), Nevado del Ruiz (Lübcke et al., 2014), Tungurahua (Warnach, 2015), and also here for Cotopaxi.

### 5.2.2 Comparison of BrO/SO$_2$ molar ratios with volcanological data

During the week after the explosions on August 14 2015, the BrO/SO$_2$ molar ratios remained on a similar low level ($\lesssim 1 \cdot 10^{-5}$) as prior to the explosions. The BrO/SO$_2$ abruptly increased to a mean value of about $4 \cdot 10^{-5}$ during the next two subsequent weeks. Gaunt et al. (2016) mentioned that the hydrothermal system might have been drying during those weeks. Accordingly, at first bromine predominately partitioned in the hydrous fluid of the hydrothermal system, but after the hydrothermal system has been dried out the bromine has probably directly partitioned to the gas phase.

The increasing trend in BrO/SO$_2$ from mid of September 2015 to early December 2015 indicates a slow but continuous change in magma pressure, magma temperature, or composition of the degassing magma body. The possible reasons are manifold.

Following Gaunt et al. (2016), the mingling of the old magma with juvenile magma could have continuously changed the effective magma composition. Or, in the case that HBr degasses at higher pressures than SO$_2$, a gradual pressure increase due to e.g. the formation of a new plug may have resulted in suppressed SO$_2$ degassing. If in contrast HBr is degassing at lower pressures than SO$_2$, the increasing trend may indicate that the magma has already degassed most SO$_2$ while the magma still...
holds significant HBr which yet has to degas. The latter interpretation would be supported by the relatively large BrO-SCDs but rather small SO$_2$-SCDs since January 2016.

5.2.3 Possible volcanological origins for the periodic pattern in the BrO/SO$_2$ molar ratios

The volcanic unrest and in particular the explosions in August 2015 distorted the volcanic system from the equilibrium thus the observed periodic pattern in the BrO/SO$_2$ data might be a manifestation of a damped and oscillating restoring process of the volcanic system to a new equilibrium. However, the damping of magma motion is rather high and thus a one-time excitement of the magma column, e.g. by the phreatomagmatic explosions in August 2015, is unlikely to cause an observable oscillation of six periods. As another possible explanation, the periodic pattern might by caused by a chance repetition of six one-time events at equidistant time intervals, e.g. by a repetitive plug formation and destruction as suggested by Gaunt et al. (2016). Anyway, even if the interpretation of a repetitive plug formation holds true, the probability that those events happened at equidistant timing is in particular rather low unless the events are triggered by a periodic external forcing. The spring-neap tide cycle of the Earth tides is such a continuous periodic forcing which, at least in principle, is continuously varying the magmatic system. The impact of the tidal forcing on magmatic systems appears to be negligibly small but might arguably play a crucial role if the geometry of the magmatic system or the surrounding host rock allow for a tide-induced "excitation" of the volcanic system, e.g. by a magma displacement or a deformation of the volcanic system. In this reasoning, the phreatomagmatic explosion in August 2015 may have (temporarily?) shifted the geometry from a non-excitable to an excitable state. A repetitive plug formation and destruction could be one consequence of such tide-induced periodic forcing but also other potential consequences (e.g. tide-induced earthquakes Ide et al. (2016), magma displacement, deformation of host rock) might result in a periodically varying degassing behaviour. Of course, we can not exclude that the unrest or geometry itself might have lead to an accidental periodicity in the activity of two weeks which was also completely independent from tidal influence, e.g. a periodic magma intrusion from the deep to the shallow reservoir due to tectonics. However, again, it appears to be unlikely that such an accidental periodicity has a period of just two weeks. Thus from all geological origins, the tidal forcing appears to be the best candidate to explain the observed periodic signal in the BrO/SO$_2$ data.

5.3 Comparison with the Earth tides

It should be kept in mind that one can expect a delay between a tide-driven process in the volcanic system and the finally observed volcanic gas emissions. We determined the delay by a cross-correlation analysis between the BrO/SO$_2$ molar ratios and the calculated tidal surface displacement. For this purpose, we shifted the time series of the Earth tide data variably by up to two week backwards in time and so manually maximised the cross-correlation coefficient between BrO/SO$_2$ and tide-induced surface displacement. However, the optimal delay is different when we optimise for the different components of the tidal signal: it is 242 h when we optimise with respect to the vertical component (or East-West component which is perfectly in phase with the vertical component) but 41 h when we optimise for the North-South component. As a result we derived correlation coefficients between the BrO/SO$_2$ molar ratios and the vertical component or the North-South component of 36 % and 47 %, respectively (see Figure 5 where both optimisation scenarios are included). As last analysis step, we dropped the
handy representation (radial, North-South, East-West) of the tide-induced surface displacement but correlated the displacement in variable directions (calculated as the component of the displacement vector in the chosen three-dimension direction) with the BrO/SO$_2$ molar ratios. The overall optimum was again found to be strictly horizontal and quite strictly to the North (optimum was 1° NNE but with similarly high correlation coefficients for ±8°) and again with a delay of 41 h.

The tidal North-South displacement component fits extraordinarily well to both, the trend and the “skewed” periodic pattern in the BrO/SO$_2$ data (left panel in Figure 6). Further, a scatter plot revealed a highly significant contrast in BrO/SO$_2$ data between small and large semi-diurnal tidal deviations, i.e. between neap tide and spring tide, respectively (right panel in Figure 6).

Figure 6. Graphical comparison of temporal variations of the BrO/SO$_2$ molar ratio and the predicted tide-induced surface displacement variation in North-South direction. Left panel: Comparison of the time series. Right panel: scatter plot which illustrates the correlation coefficient of 47 % between both time series, the gradual changing colour of the data points gives the measurement date from red (September 8 2015) to blue (December 15 2015).

A possible explanation for this preferred direction may be found, in general, in the local fault geometry at Cotopaxi which are E-W-striking normal faults and NNE-SSW-striking vertical strike-slip faults (Fiorini and Tibaldi, 2012) and, with respect to the particular period of unrest, in the inclined sheet intrusion prior to the eruption located southwest of the summit (Morales Rivera et al., 2017). If the fault systems are close to a “kinematically critical point”, the horizontal tidal displacements, and in particular those in the N-S direction, may distort the local pressure regime sufficiently to trigger enhanced fault dynamics (i.e. alternating contractional and extensional stresses) which in turn induce stress variations in the conduit wall-rocks and the magma reservoir. E.g. both fault bodies may adapt slightly differently to the additional horizontal forcing in N-S direction which may result in a slightly loosening between the wedged footwall and hanging wall and as a consequence enhance the slip velocity during a spring tide compared to neap tide. The additional fault dynamics may periodically cause e.g. micro-earthquakes (Ide et al., 2016) or variations in the geometry of the volcanic system.

6 Conclusions

During the Cotopaxi unrest 2015, we observed a periodic pattern with a period of 13.7 days in the BrO/SO$_2$ molar ratios within the volcanic gas plume of Cotopaxi. Despite the fact that the analysed time interval spans just over six periods of this signal, the
statistical significance is unexpectedly high (false alarm probability of 0.9 % and detection confidence of about 90 %). At first, we examined the variability of the meteorological conditions as origin for the periodic variation of the BrO/SO$_2$ molar ratios. We found that the relative humidity exhibits a similar long-term trend as the BrO/SO$_2$ molar ratios and the trend was further superimposed for half of the time interval by a periodic pattern with a 13.1 days periodicity. Therefore the periodic pattern in the BrO/SO$_2$ data may be partially explained by the variations in the relative humidity, however, the cross-correlation coefficient was only 33 % or less. Also a local repetition of independent one-time events cannot be ruled out from the list of possible origins, however, the probability for those to occur equidistantly in time all 13.7 days is exceedingly low. Therefore the Earth tidal forcing appears to be the most promising explanation for the observed periodical BrO/SO$_2$ variations, where correlation coefficients of 36 % and 47 % were found between the BrO/SO$_2$ molar ratios and the vertical and North-South components of the tide-induced surface displacement, respectively.

Whether or not the presented data show a manifestation of the Earth tides or are due to some other cause is yet difficult to answer as we only observed six periods. The observed periodicity of 13.7 days would support a mechanism which is linked to the North-South component of the tides, e.g. an amplification of the oscillation by a North-South displacement of the host rock, rather than a mechanism which is linked to the much larger tide-induced vertical displacement. Nevertheless, the NOVAC dataset allows to undertake large-scale statistical analyses on this topic. Thus long time-series at a particular volcano might give a deeper insight in the origin of such signals. Future studies will undertake a global comparison of different volcanoes and might reveal which geological geometries are excitable by the tidal forcing.

**Appendix A: Theoretical background on Earth tides**

Gravitational forcing caused by the Moon and the Sun in their interaction with the Earth varies with time. The resulting tidal potential (i.e. the residual gravitational potential) is a function of location and time and depends on all astronomical motions such as orbit, rotation, and precession of the involved bodies. The periodicities of these parameters have been studied since millenia and are well known. Already in the 1880s the tidal potential could be calculated to high precision by a harmonic decomposition (Darwin, 1883) and (Doodson, 1921), i.e. as a sum of an infinite number of harmonic oscillators with accurately known angular frequencies $\omega_i$ and amplitudes $a_i$. In the literature, the amplitudes of the tidal harmonics are conventionally noted as the (theoretical) vertical displacement $\Delta z_i = \frac{a_i}{g_{std}} \cdot R_{eq}$ of the Earth’s surface at the equator, with respect to the equatorial Earth radius $R_{eq} = 6378$ km and the conventional standard gravitational acceleration $g_{std} = 9.80665 \frac{m}{s^2}$, caused by the forcing of the particular tidal harmonic (Agnew, 2007). The tidal harmonics with the largest displacement amplitudes are summarised in Table A1. Hereby, the strength of a particular tidal harmonics varies with latitude: The semi-diurnal tides are maximum at the equator and the poles but vanish at mid-latitudes. The diurnal tides are maximum at the mid-latitudes but vanish at the equator and poles. The long-term tides are maximum at the equator and vanish at the poles.

Cotopaxi is located at the equator, thus only the semi-diurnal and long-term tides are contributing. Further, the time scale of the solar cycle (M0) is beyond the time scale of our observation and the amplitude of the lunar cycle (Mf) is rather negligible com...
Table A1. Strongest tidal harmonics (Agnew, 2007). The tide species describes its dependency on latitude (see text for details). The Darwin Symbols are a set of conventional notation, the amplitude gives the theoretical amplitude of the periodical vertical displacement of the Earth’s surface which would be caused by this particular tidal harmonic alone. The frequency is given in cycles per day and the length of the period is given in days. The set is divided by the horizontal bars in semi-diurnal, diurnal, and long-term harmonics.

<table>
<thead>
<tr>
<th>Tide species</th>
<th>Darwin Symbol</th>
<th>Amplitude [m]</th>
<th>Frequency [cpd]</th>
<th>Length of Period [d]</th>
</tr>
</thead>
<tbody>
<tr>
<td>semi-diurnal</td>
<td>M2</td>
<td>0.63221</td>
<td>1.9322736</td>
<td>0.5175251</td>
</tr>
<tr>
<td></td>
<td>S2</td>
<td>0.29411</td>
<td>2.0000000</td>
<td>0.5000000</td>
</tr>
<tr>
<td></td>
<td>N2</td>
<td>0.12105</td>
<td>1.8959820</td>
<td>0.5274312</td>
</tr>
<tr>
<td></td>
<td>K2</td>
<td>0.07991</td>
<td>2.0054758</td>
<td>0.4986348</td>
</tr>
<tr>
<td>diurnal</td>
<td>K1</td>
<td>0.36864</td>
<td>1.0027379</td>
<td>0.9972696</td>
</tr>
<tr>
<td></td>
<td>O1</td>
<td>0.26223</td>
<td>0.9295357</td>
<td>1.075806</td>
</tr>
<tr>
<td></td>
<td>S1</td>
<td>0.12199</td>
<td>0.9972621</td>
<td>1.002745</td>
</tr>
<tr>
<td>long-term</td>
<td>M0</td>
<td>0.31459</td>
<td>0.0000000</td>
<td>(1 year)</td>
</tr>
<tr>
<td></td>
<td>Mf</td>
<td>0.06661</td>
<td>0.0732022</td>
<td>13.66079</td>
</tr>
</tbody>
</table>

Compared to the semi-diurnal tides. Because the two dominant semi-diurnal tidal harmonics, the lunar semi-diurnal (M2) and the solar semi-diurnal (S2), have slightly different periodicities, their interference results in the so-called “spring-neap tide cycle” which has a period of 14.75 days and is the strongest periodic long-term pattern of the tidal forcing. This interference results at the equator in a vertical surface displacement of about ±1 m during spring tide (M2+S2) and about ±0.3 m during neap tide (M2-S2). The additional contribution of the other semi-diurnal tidal harmonics (N2,K2) slightly vary this displacement. Phenomenologically, the spring tide occurs when Moon, Sun, and Earth are perfectly aligned, i.e. at new moon and full moon.

The compartments of the Earth respond on the temporal changes of tidal potential according to their mechanical properties such as their viscosity and compressibility. The water in the oceans responds to variations of the tidal forcing almost immediately and is thus displaced always with the theoretical value, e.g. ±1 m at spring tide. Solid rock responds much slower and is thus displaced by only about 0.2980 (radial Love number of the SNREI Earth, (Agnew, 2007)) times the theoretical value, e.g. ±0.3 m at spring tide. Magmatic melt is less viscous than solid rock and may therefore adopt faster to the tidal potential. Accordingly, the tidal forcing should lead to a relative displacement between magma in a conduit and the containing host rock.
Appendix B: Experimental Data: Methods and Measurement

B1 DOAS and NOVAC

Differential Optical Absorption Spectroscopy (DOAS) (Platt and Stutz, 2008) is an analysing technique which is suitable for remote sensing of volcanic gas plumes. The output of DOAS are the simultaneously retrieved slant column densities (SCD) of a set of volcanic trace gases. The SCDs are the integral of the particle density of the particular gas along the light path. Together with additional information on the expansion of a volcanic gas plume and the wind conditions, the particle density and even the emission fluxes of volcanic trace gases like SO$_2$ and BrO can be retrieved from the SCDs. In this manuscript, we are focusing on the BrO/SO$_2$ molar ratio in volcanic gas plumes, i.e. non of those additional information is required. At volcanoes, usually scanning DOAS systems are used because these can provide a spatial coverage from horizon to horizon with a good temporal resolution. The instruments in the Network for Observation of Volcanic and Atmospheric Change (NOVAC) were designed in an autarkic and simple set-up in order to match the harsh conditions and remote locations of volcanoes (Galle et al., 2010). As a drawback, NOVAC instruments do not have an active temperature control as the power supply by solar panels is limited. Prior to each scan (~ 5 – 15 min), the measurement routine adjusts the exposure time to the meteorological conditions. As the main goal of NOVAC is the monitoring of volcanic SO$_2$ fluxes, the number of consecutive exposures is manually fixed aiming for the best compromise between precision and temporal resolution of the SO$_2$ measurement. While this leads typically to a precision of the SO$_2$ retrieval in the percent range, the setting is not optimal for the BrO retrieval. Nonetheless, Lübcke et al. (2014) have shown that also BrO can be retrieved from NOVAC instruments by applying an advanced evaluation algorithm. Thus NOVAC allows, for the first time, to determine long-term time series of BrO/SO$_2$ molar ratios at a large number of volcanoes.

B2 Retrieval of BrO/SO$_2$ molar ratios from NOVAC data: Plume detection and optimising the BrO detection limit

For all spectroscopic retrievals of SO$_2$ and BrO, we applied the DOAS fit scenarios described by Lübcke et al. (2014) and also most evaluation steps were applied identically. In the first evaluation step, all spectra from a horizon-to-horizon scan are pre-evaluated for SO$_2$ using its particular zenith spectrum as reference spectrum. The result is a SO$_2$-SCD distribution as a function of the viewing angle. While the precision of the SO$_2$ data allows for a spatial analysis of the volcanic plume, the optical density of BrO in a volcanic gas plume is at least one order of magnitude smaller than for SO$_2$ and thus a higher photon statistic is required. This is realised by a subsequent adding of spectra which are recorded in the temporal proximity and in the same or at least similar viewing direction.

Accordingly, we used the SO$_2$-SCD distribution to identify all spectra which are predominately part of the volcanic plume, i.e. with only little dilution, and add the spectra in order to get one “added plume spectrum per scan”. The drawback of this method is the loss of spatial information as the retrieval gives only one mean plume value for the BrO-SCDs or the BrO/SO$_2$, respectively. A volcanic gas plume can be assumed to have an about Gaussian shaped angular gas distribution embedded in a flat, gas free reference region. (The reference region might be differing from zero SO$_2$ as the arbitrary picked reference spectrum might contain gas. However, on this stage only the angle-dependent shape and not the quantitative value is of interest.)
For their proof of concept, Lübcke et al. (2014) ignored this reasonable assumption of the plume shape and simply defined the plume region as the angle region (≥ 33°) with the highest running mean value over 10 spectra for the SO$_2$-SCDs. For relatively narrow volcanic plumes this fixed plume region may contain also viewing directions where the volcanic plume has been significantly diluted, and therefore the “added plume spectrum” would contain also a significant contribution from the reference region and thus underestimate the SO$_2$-SCD in the real plume. To improve the accuracy, we instead fit a Gaussian distribution on the angular SO$_2$-SCD distribution in order to routinely separate all pure plume spectra from significantly diluted spectra. The 1-σ range of the Gaussian distribution is then defined as the plume region. When no or only a partial plume is detected (concretely, if the Gauss fit does not succeed or when the 1-σ range of the Gaussian fit was less then 5°) the scan is rejected from the further analysis. On the other hand, when the 1-σ range is expanding more than 33° (67% of scans for the presented data), the plume region is defined as by Lübcke et al. (2014). Similarly and in accordance with Lübcke et al. (2014), the 10 spectra of the scan with the lowest SO$_2$-SCDs are considered as gas-free background spectra and are added up to one “added reference spectrum per scan”.

In the next step, for each scan a SO$_2$ and a BrO DOAS-fit has been performed based on the added plume spectrum and added reference spectrum. In order to further improve the signal-to-noise of the BrO fits, the added plume spectra of four consecutive scans are added up to “multi-scan plume spectra”, however, only those scans with $\chi^2$(BrO fit) < 10$^{-3}$ (∼ 95% of all suitable scans) were considered in order to avoid the influence of relatively bad scans. Analogue, also multi-scan reference spectra were obtained. The final BrO data have for periods with significant BrO degassing a mean temporal resolution of 10 (and up to ∼ 30) data points per day and a standard deviation of about 3 · 10$^{13}$ molec cm$^{-2}$. The standard deviation is estimated as two times the DOAS fit error of the multi-scan BrO fit (Stutz and Platt, 1996). The SO$_2$ detection limit of the final data is in the order of 1 · 10$^{16}$ molec cm$^{-2}$, i.e. the precision of the SO$_2$ data is still about a factor of 100 better than for BrO and thus within the scope of BrO/SO$_2$ molar ratio calculation considered as exactly measured.

The BrO detection limit can be further enhanced by e.g. daily averaging to dynamic values of BrO$^{DT} = \frac{3}{\sqrt{n}} \cdot 10^{13}$ molec cm$^{-2}$ (with $n$ the number of “multi-scan” data points per day), but anyway, most retrieved BrO-SCDs are below the detection limit. However, a blindfold rejection of all data with BrO-SCDs below the detection limit would not only drastically reduce the number of available data but would also select those scans when the BrO-SCDs is particularly high. As such a selection leads to systematically overestimated molar ratios, a more careful selection criteria is required for more accurate BrO/SO$_2$ molar ratio calculation (Lübcke, 2014). As we are actually not interested in the BrO-SCDs but the BrO/SO$_2$ molar ratios, we set our criteria in order to increase the reliability of observed (low) molar ratios. For this purpose we define periods of strong degassing as above an SO$_2$-SCDs threshold level of SO$_2$thres$ = 7 \cdot 10^{17}$ molec cm$^{-2}$ and select only those data which are above the threshold. Within those data, the detection limit of the BrO/SO$_2$ molar ratios is (BrO/SO$_2$)$^{DT} = \frac{\text{BrO}^{DT}}{\text{SO}_2^{\text{thres}}}$ = $\frac{4}{\sqrt{n}} \cdot 10^{-5} \leq 1 \cdot 10^{-5}$. So for the chosen data set, we are able do distinct whether the molar ratio is below or above its detection limit. The SO$_2$ threshold is chosen as best compromise between a low BrO/SO$_2$ detection limit and sufficient amount of data passing the criteria. For observed SO$_2$-SCDs further above the threshold also the BrO/SO$_2$ detection limit further decreases.
B3 Alternative SO$_2$ fit range for untypically strong SO$_2$ emissions

The approximations which are applied in the DOAS algorithm are only justified for weak absorbers, i.e. if the investigated optical density is below $\sim 0.1$. For a larger optical density, the DOAS approach usually underestimates the SCD of the investigated trace gas. For the “standard” (i.e. following Lübcke et al. (2014)) SO$_2$ fit range from 314.8 - 326.8 nm, SO$_2$ can be considered to be a weak absorber for SCDs of up to $\sim 1 \cdot 10^{18}\text{molec cm}^{-2}$ but the SO$_2$-SCD gets increasingly underestimated with increasing optical densities. For most NOVAC data, the SO$_2$-SCDs are not exceeding this threshold significantly, however, during the Cotopaxi unrest 2015 SO$_2$-SCDs of up to the order of $1 \cdot 10^{19}\text{molec cm}^{-2}$ have been observed. For more accurate SO$_2$-SCDs, we re-evaluated the "multi-scan plume spectra" with an alternative fit range from 326.5 - 335.3 nm which has been suggested by Hörmann et al. (2013) in order to evaluate SO$_2$-SCDs up to about $1 \cdot 10^{19}\text{molec cm}^{-2}$. As drawback, the SO$_2$ measurement error is here drastically increased with relative values of about 10 %, i.e. about $1 \cdot 10^{18}\text{molec cm}^{-2}$ for the extreme SCDs. In order to pick the most reliable data, we use by default the results of the "standard" SO$_2$-fit but switch to the "alternative" fit if the discrepancy between both fit results is larger than four times the fit error of the alternative fit (thus about two times the measurement error of the SO$_2$-SCD, Stutz and Platt (1996)), i.e. if the discrepancy is more than about $2 \cdot 10^{18}\text{molec cm}^{-2}$.

B4 Challenges when applying the oxygen dimer O$_4$ and Colour Index retrieval on NOVAC data

Established cloud detection algorithms base on the absorption of the oxygen dimer O$_4$ at 360 nm or the relative intensity ratio of the intensity of the backscattered solar radiation at 320 nm and 440 nm (see e.g. Wagner et al. (2014)). The application of those or similar algorithms on NOVAC data faces at least three challenges: (1) The effectively detected wavelengths range from 280 nm to 400 nm, however, with a linear decrease in transmittance already from 370 nm to 400 nm due to the HOYA U330 UV bandpass filter. Accordingly, the standard colour index pair is not applicable. (2) The measurement routine automatically optimises the integration time of the spectra with respect to the wavelength range of the SO$_2$ retrieval ($\sim 310 - 335$ nm). As drawback, spectra are often, in particular at cloud free days, over-saturated starting a 365 nm but sometimes even already at 359 nm. Accordingly, the standard O$_4$ retrieval is typically not applicable on NOVAC data when the sky is cloud free. On the other hand, the absorption signal of the O$_4$ line at 344 nm is not significant for a spatial analysis. (3) Many NOVAC instruments (at Cotopaxi three of four) use a conical scan geometry thus never record zenith spectra. Missing the zenith value for O$_4$ or the colour index makes the interpretation of the analysis results more challenging.

We anyway tested both methods on the NOVAC data retrieved from the Cami station (because there zenith information is available). For the colour index analysis, we compared the mean intensity of the wavelength ranges at 329-329.7 nm and at 381-381.6 nm (each the average of 10 detector channels, see also Lübcke (2014)). We applied the analysis on the zenith spectra of each particular scan. The resulting time series of the colour index has not shown any periodic pattern and most long-term variations were small compared to the mean daily variations (see Figure A1 upper panel). For the O$_4$ retrieval, we applied a fit scenario with the same absorbers as for BrO (see Lübcke et al. (2014)) but with a fit range from 338 nm to 365 nm. We
applied the analysis on the individual spectra within each scan and used the particular zenith spectrum as reference spectrum. A comparison with the results of the SO$_2$ retrieval showed no correlation, i.e. no systematic enhancement or reduction of O$_4$ absorption signal has been observed within the volcanic plume.

As additional approach, we applied the same O$_4$ analysis on the multi-scan plume spectra recorded by all NOVAC stations at Cotopaxi and used the particular multi-scan reference spectrum as reference spectrum. The resulting time series neither contained periodic patterns nor showed a significant correlation with the BrO/SO$_2$. On the other hand, the stations Refugio and Refugio Sur, where the plume is typically passing at lower elevation angles, found O$_4$ enhancements by about $2 \cdot 10^{12}$ molec cm$^{-2}$ in the plume while the stations Cami and San Joaquin, where the plume is typically passing in about zenith direction, found no O$_4$ enhancement in the plume (see Figure A1 lower panel). This enhancement is probably solely due to the dependency of the background O$_4$ slant column density on the elevation angle, illustrating the difficulty to interpret the O$_4$ results. We want to highlight that more sophisticated and well validated studies which e.g. take use of massive filtering of the data may indeed retrieve information of the aerosol load from the NOVAC data, however, the development of such a sophisticated cloud classification algorithm is beyond the scope of this study.

**Acknowledgements.** We would like to thank the European Commission Framework 6 Research Program for funding of the NOVAC project. We kindly acknowledge the staff at IGEPN for keeping the instruments running at Cotopaxi. We thank the Deutsche Forschungsgemeinschaft for supporting this work within the project DFG PL193/14-1. Nicole Bobrowski thanks for financial support from DFG BO 3611/1-2 and the VAMOS project. Florian Dinger thanks ECMWF for providing the meteorological data and Steffen Dörner (MPIC) for assisting with the ECMWF data.
Figure A1. Upper panel: Colour Index (here: mean intensity of the wavelength ranges at 329-329.7 nm and at 381-381.6 nm) retrieved from Cami station. The analysis based on the single scans, shown are the daily averages and the error bars indicate the standard deviations of the daily variations. Lower panel: Different of the O$_4$ slant column density in the plume region and the reference region (as found from the SO$_2$ analysis, see Appendix B2). The O$_4$ enhancement observed by the stations Refugio and Refugio Sur is probably just due to the dependency of the background O$_4$ slant column density on the elevation angle.

References


